# Viscosity Dependence of Polystyrene Local Dynamics in Dilute Solution

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ABSTRACT: Variable-temperature  $^2H$  NMR  $T_1$  measurements have been performed on backbone-deuterated atactic polystyrene at two Larmor frequencies in four solvents: toluene, cis-decalin, dibutyl phthalate, and dioctyl phthalate. The time integral  $\langle\sigma\rangle$  of the C–D vector orientation correlation function is extracted from the  $T_1$  data without assuming a specific model for C–D vector reorientation. The hydrodynamic Kramers' theory in the high-friction limit cannot describe the viscosity and temperature dependence of  $\langle\sigma\rangle$ . In contrast,  $\langle\sigma\rangle$  is found to have a power law dependence on solvent viscosity with an exponent of  $0.76\pm0.05$ , whether the viscosity is varied by changing solvent or temperature. The internal energy barrier for polystyrene C–D vector orientation is determined to be  $14\pm3$  kJ/mol using the power law viscosity dependence. The inapplicability of Kramers' theory is attributed to the lack of a clear separation between the time scales of polymer and solvent motions. As expected on the basis of this explanation, the viscosity exponents for polystyrene and five other polymers are found to correlate with the molecular weight of the side groups.

#### I. Introduction

The relationship between polymer properties and structures is a major theme of polymer science. The local segmental motions of polymers play an important role in understanding one important structure—property relationship. Dynamics on the scale of a few monomer units depend strongly on the polymer structure and have long been associated with molecular weight independent properties such as  $T_{\rm g}$ , physical aging, and the temperature dependence of the viscosity.

Since the interactions between polymer chains are minimized in dilute solution, this environment has often been used to isolate the intramolecular factors which control local polymer dynamics. Kramers' theory<sup>1,2</sup> has been the conventional framework for understanding local polymer dynamics in dilute solution. This theory predicts that these dynamics have a linear dependence on solvent viscosity. Recent work  $^{3-6}$  has shown that Kramers' theory is not applicable for at least some polymers. Instead of a linear dependence on solvent viscosity, local polymer relaxation times are found to have an apparent power law dependence. The use of Kramers' theory where it is not applicable can lead to serious errors in the determination of the potential energy barrier between different conformational states.<sup>3,4</sup> This potential energy barrier has been postulated to be one of the most important parameters determining  $T_{g}$ for bulk polymers.

The power law exponent which describes the dependence of local dynamics upon solvent viscosity has been observed to increase with the mass of the polymer side group. For example, in *cis*-1,4-polybutadiene,³ the correlation time for C–H vector reorientation is proportional to solvent viscosity raised to the power 0.33; the exponent is 0.41 for polyisoprene<sup>4</sup> (PI) and 0.43 for 1,2-polybutadiene<sup>5</sup> (1,2-PB). This trend has been rationalized by the observation that high-frequency local motions are opposed by a friction which is smaller than that calculated from the zero-frequency viscosity.<sup>4</sup> This explanation predicts that the viscosity exponent will

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become 1 (i.e., Kramers' theory will be applicable) when the side group becomes sufficiently large that its motion is determined by the zero-frequency viscosity. How large must side groups be for Kramers' theory to be applicable? We address this question by performing experiments on polystyrene (PS). Analysis of literature data over a limited viscosity range indicates that PS has a viscosity exponent close to one and thus Kramers' theory is applicable.<sup>5</sup> Here we check this conclusion with a systematic study covering a wider range of solution viscosities.

We report here the results of  ${}^{2}H$  NMR  $T_{1}$  measurements on backbone-deuterated atactic polystyrene (PS $d_3$ ) in four solvents at two Larmor frequencies. The experimental data are analyzed in the extreme narrowing regime so that no model for the reorientation of C-D vectors needs to be assumed. Our analysis shows that Kramers' theory cannot describe the local dynamics of PS. Instead of having a linear dependence on solvent viscosity  $\eta$ , the time integral  $\langle \sigma \rangle$  of the C-D vector correlation function scales with  $\eta^{0.76}$ . Using the power law viscosity dependence, we found that the activation energy of PS local motions is  $11 \pm 1$  kJ/mol in toluene and  $15 \pm 2$  kJ/mol in other solvents. Reanalysis of literature data on PS solutions gives approximately the same activation energies. The viscosity exponents for various polymers are found to correlate with the mass of the side group.

Comparison of  $T_1$  data at multiple Larmor frequencies also yields information about the shape of the C–D vector orientation autocorrelation function. These results are discussed elsewhere.<sup>7</sup>

## **II. Experimental Section**

**Materials.** Backbone-deuterated atactic polystyrene (PS- $d_3$ ,  $M_{\rm w}=56\,000$ ;  $M_{\rm n}=27\,000$ ) was purchased from Cambridge Isotope Lab. Low molecular weight impurities were eliminated from the polymer by fractional precipitation using methyl ethyl ketone as a good solvent and methanol as a poor solvent. The precipitated polymer was placed under vacuum at 373 K for 2–3 h to remove trace solvent. We expect that the purified polymer has  $M_{\rm w}$  somewhat higher than 56 000. For flexible polymers, it has been established that local dynamics are independent of molecular weight when the

**Table 1. Solvent Viscosities** 

T(K)	η (cP)	T(K)	η (cP)
	Dibutyl F	hthalate	
374	2.13	407	1.29
394	1.57	421	1.09
	Dioctyl P	hthalate	
376	3.82	407	2.15
392	2.78	420	1.76

polymer molecular weight exceeds roughly  $10,000.^8$  Therefore the  $T_1$  data presented here represent those of a high molecular weight polystyrene sample.

Toluene, *cis*-decalin, di-*n*-butyl phthalate (DBP), and bis-(2-ethylhexyl) phthalate (DOP) were purchased from Aldrich (purity  $\geq$  99%) and were used as received. Except as noted below, the viscosities of the solvents are reported in the literature. 9-11 The kinematic viscosities of DBP and DOP from 370 to 420 K were measured using a Cannon-Fenske capillary flow viscometer. Absolute viscosities were calculated assuming that the temperature dependence of DBP and DOP densities follows that given in ref 11. The results are shown in Table 1. At 380 K, the four solvents cover a viscosity range of more than one decade.

With one exception, the polymer concentration in all solutions was of  $10 \pm 1\%$  (w/w). Some measurements were performed on a 3% solution in order to determine the dependence of  $T_1$  on concentration. All samples were degassed prior to being sealed under vacuum.

**NMR Measurements.** Deuterium  $T_1$  measurements were performed at 76.86 and 15.37 MHz on Bruker AM-500 and AC-100 spectrometers, respectively. A standard inversion—recovery—fid pulse sequence was employed. The recovery of the  $^2$ H magnetization was always exponential. The temperature was stable within  $\pm 1$  K.  $T_1$  data at 76.86 and 15.37 MHz are reproducible within  $\pm 1\%$  and  $\pm 4\%$ , respectively.

We attempted NMR measurements from the highest possible temperatures to temperatures well below the  $T_{\rm I}$  minima. The high-temperature limit for each solvent was set either by the solvent boiling point or the NMR probe (limited to 425 K). The low-temperature limit for the 10% PS/toluene solution was set by phase separation at around 233 K. PS/DOP solution and PS/cis-decalin solutions were phase-separated below 233 and 268 K, respectively.

Only one peak was observed in  $^2H$  NMR spectra over the entire temperature range of the experiments in all solvents. Therefore the  $T_1$  data measured reflect the average behavior of the methine and methylene deuterons.  $^{13}C$   $T_1$  measurements on PS solutions indicate that backbone methylene and methine C–H vectors reorient at the same rate.  $^{12}$  Thus we expect that the two kinds of backbone C–D vectors have very similar dynamics and that the conclusions in this paper apply to both of them.  $^{13}$ 

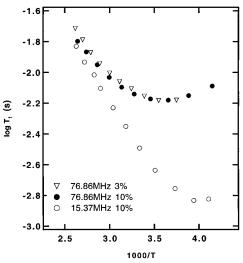
**Data Analysis.** The reorientation of a C-D bond may be characterized by its orientation autocorrelation function. NMR  $T_1$  measurements are sensitive to the second-order correlation function:

$$G(t) = \frac{1}{2} \langle 3(\mathbf{e}_{x}(t) \cdot \mathbf{e}_{x}(0))^{2} - 1 \rangle \tag{1}$$

Here  $\mathbf{e}_x(t)$  is a unit vector in the direction of the C-D bond at time t. The brackets indicate an ensemble average. The shape of the correlation function is determined by the specific mechanism of C-D vector reorientation and will be discussed elsewhere.<sup>7</sup> The rate of C-D vector reorientation may be characterized by a model-independent quantity  $\langle \sigma \rangle$ , <sup>14</sup> which is the time integral of the correlation function G(t):

$$\langle \sigma \rangle = \int_0^\infty G(t) \, \mathrm{d}t \tag{2}$$

We discuss the dependence of  $\langle \sigma \rangle$  on solvent viscosity and temperature in this paper.



**Figure 1.** <sup>2</sup>H  $T_1$  values for PS- $d_3$  in toluene vs temperature. Different symbols represent different concentrations and Larmor frequencies. The 15.37 MHz data above 3 ms (log  $T_1$ = -2.52) are taken to be in the extreme narrowing region.

Deuterium nuclear magnetization is relaxed by electric quadrupole coupling. In the extreme narrowing region,  $T_1$  is related to  $\langle \sigma \rangle$  by the following equation: <sup>15,16</sup>

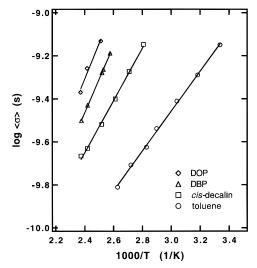
$$\frac{1}{T_1} = \frac{3}{2}\pi^2 (e^2 q Q/h)^2 \langle \sigma \rangle \tag{3}$$

where  $e^2qQ/h$  is the  $^2H$  quadrupole coupling constant. Consistent with previous work, we chose  $e^2qQ/h$  to be 172 kHz for PS backbone deuterons.  $^{8,17,18}$  The uncertainty in this number is expected to be less than 5%. We define the extreme narrowing region by the observation that  $T_1$  is independent of Larmor frequency. Another criterion often used is that  $T_1 = T_2$ .  $^{8,19}$  Because  $T_2$  is sensitive to very low frequency motions such as the reorientation of the whole polymer chain,  $T_1$  is generally not equal to  $T_2$  for polymers. These very slow motions have little effect on  $T_1$  and account at most for the last few percent of the decay of G(t). The  $\langle \sigma \rangle$  obtained from eq 3 under these conditions represents an average of all fast motions; i.e., the upper limit of integration in eq 2 is replaced by  $(1/\omega_D)$ , where  $\omega_D/2\pi$  is the deuterium Larmor frequency.

The calculation of  $\langle \sigma \rangle$  using eq 3 is not based on any assumption about the shape of the correlation function. For comparison, we have also calculated  $\langle \sigma \rangle$  by the integration of modified  $\log \chi^2$  correlation functions generated from fitting all the experimental data (including data not in the extreme narrowing region);<sup>7</sup> these results will be discussed below.  $\langle \sigma \rangle$  values used throughout this paper are calculated from eq 3 unless otherwise specified. The conclusions in this paper about  $\langle \sigma \rangle$  are believed to be independent of whatever model might be used to fit G(t).

### **III. Results and Discussion**

Figure 1 shows  $^2$ H  $T_1$  values for PS- $d_3$  in toluene as a function of temperature. We first address the issue of polymer concentration. At 76.86 MHz, to the left side of the  $T_1$  minima, the 3% polymer solution has  $T_1$  values slightly longer than the 10% solution. This indicates that C-D vectors reorient slightly faster in 3% solution than in 10% solution. It has been established that  $T_1$  values for flexible polymers are almost independent of concentration up to 15%, despite the enormous increase in the solution viscosity. For PS, a threefold concentration increase shortens  $T_1$  by 10% or less. The following discussion is all based on 10% solutions. We expect that the conclusions drawn from this work on 10% solutions will also be applicable to lower concentration solutions.



**Figure 2.** Time integral of C-D vector correlation function  $\langle \sigma \rangle$  vs temperature in different solvents.  $\langle \sigma \rangle$  is calculated from 15.37 MHz data in the extreme narrowing region (see eq 3).

Figure 1 also allows us to estimate the limits for the extreme narrowing region. At 382 K (1000/T = 2.62),  $T_1$  data at two Larmor frequencies are within  $\pm 5\%$  of 15 ms, which means that the extreme narrowing condition is approximately met when  $T_1$  is longer than 15 ms at 76.86 MHz. Given that the two Larmor frequencies are different by a factor of 5, we may extend this 15 ms limit by a factor of 5, and approximate the extreme narrowing condition at 15.37 MHz as the region where  $T_1$  is longer than 3 ms. The same criterion has been applied to  $T_1$  data in other solvents;  $\langle \sigma \rangle$  values have been calculated from  $T_1$  values at 15.37 MHz using eq 3.

Figure 2 shows the calculated  $\langle \sigma \rangle$  versus temperature in different solvents. At a given temperature, higher viscosity solvents such as DBP and DOP naturally show larger  $\langle \sigma \rangle$ , indicating slower motions. The rest of this paper discusses the data illustrated in Figure 2. All  $T_1$ data may be found in the supporting information.

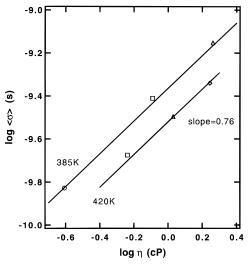
Inapplicability of Kramers' Theory. Kramers' theory describes the rate at which a particle passes over an energy barrier under the influence of Gaussian random forces. 1 It has often been applied to polymer local dynamics in dilute solution. In this context, and in the high-friction limit, Kramers' theory predicts  $that^{20-23}$ 

$$\langle \sigma \rangle = A \eta \, \exp \left( \frac{E_{\rm a}}{RT} \right)$$
 (4)

Here A is a constant and  $E_a$  is usually interpreted as the average potential energy barrier between conformational states.

Equation 4 can be tested in two ways using data shown in Figure 2. Constant-temperature plots of  $\log \langle \sigma \rangle$ vs log  $\eta$  are presented in Figure 3. Since there is no one temperature where  $\langle \sigma \rangle$  values are available for all four solvents, we chose two temperatures in order to use data from all solvents, with the data for three solvents being used at each temperature. The slopes of the two lines in Figure 3 are 0.76. This is not consistent with Kramers' theory, which predicts a slope of 1. Thus eq 4 is incapable of describing the viscosity dependence of  $\langle \sigma \rangle$  at constant temperature.

Equation 4 may be further tested by varying the temperature. We plot  $\log (\langle \sigma \rangle / \eta)$  vs the inverse of temperature in Figure 4. Instead of a master curve of



**Figure 3.** Logarithm of  $\langle \sigma \rangle$  vs the logarithm of solvent viscosity at constant temperature. The two lines have a slope of 0.76. In contrast, Kramers' theory in the high-friction limit predicts a slope of 1. Solvent symbols are the same as in Figure

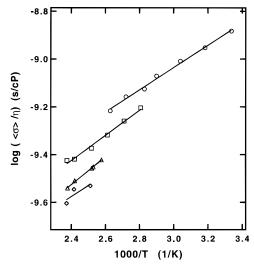


Figure 4. Test of Kramers' theory (eq 4) using C-D vector reorientation times  $\langle \sigma \rangle$  in various solvents. Solvent symbols are the same as in Figure 2. Different solvents have different lines, which suggests that Kramers' theory cannot describe the behavior of C-D vector reorientation of PS-d3 in dilute solution.

all four solvents, as predicted by eq 4, data from the four solvents fall on four different lines. Although one may argue that the preexponential factor A may be different in different solvents, we know of no reason why A should vary with solvent viscosity systematically.

Nonlinear Viscosity Dependence. Previous investigations have found<sup>3-6</sup> that  $\langle \sigma \rangle$  often has a power law dependence on solvent viscosity:

$$\langle \sigma \rangle = A \eta^{\alpha} \exp\left(\frac{E_{\rm a}}{RT}\right) \tag{5}$$

Figure 3 has shown that at 420 and 385 K,  $\alpha$  is 0.76  $\pm$ 0.05. We may further test eq 5 by varying temperature. Thus we plot  $\log (\langle \sigma \rangle / \eta^{0.76})$  vs the inverse of temperature in Figure 5. Data from the four solvents form a master curve. Although not perfect, the power law viscosity dependence does provide a reasonable fit to the experimental data. The average  $E_a$  calculated using eq 5 is  $14 \pm 3$  kJ/mol.

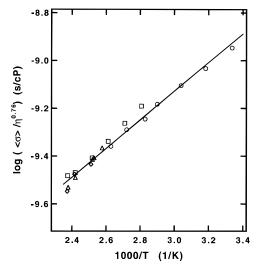


Figure 5. Test of the power law viscosity dependence using the viscosity exponent extracted from Figure 3. Solvent symbols are the same as in Figure 2. Different solvents fall on the same line, indicating that the power law viscosity dependence is a reasonable description of PS local dynamics in dilute solution.

Careful examination of Figure 5 reveals that the local dynamics of PS seem to have slightly different activation energies in different solvents.  $E_a$  is equal to  $11 \pm 1 \text{ kJ/}$ mol in toluene,  $13 \pm 1$  kJ/mol in *cis*-decalin,  $16 \pm 1$  kJ/ mol in DBP, and  $14 \pm 3$  kJ/mol in DOP.  $E_a$  values for PS in DBP and toluene are clearly different. In contrast,  $E_a$  does not depend upon solvent for other polymers such as cis-1,4-polybutadiene<sup>3</sup> and polyisoprene.<sup>4</sup> The variations observed for E<sub>a</sub> values for PS may be due to specific interactions between the polymer and the solvents.

The inapplicability of Kramers' theory is most likely due to the lack of a separation in time scales for the polymer and solvent motions. Kramers' theory is derived from the Langevin equation. One important assumption when applying the Langevin equation is that the system dynamics are significantly slower than the bath dynamics. For the case of a dilute polymer solution, the polymer is the system and the solvent is the bath. If a conformational transition proceeds slowly (relative to the solvent motions), then at each point along the reaction coordinate the solvent is able to equilibrate to the new positions of the chain atoms. In this case the friction impeding the polymer's conformational transition is proportional to the zero-frequency solvent viscosity and the high-friction Kramers' theory should be applicable. For *cis*-1,4 polybutadiene<sup>3</sup> and polyisoprene<sup>4</sup> in dilute solution, it has been shown that local polymer motions are comparable and sometimes even faster than the solvent motions. For PS- $d_3$ , it is likely that the time scale separation between polymer and solvent motions is also not large enough to make the Langevin equation valid. We note that for poly(1naphthylmethyl acrylate) (PNMA),24 whose motions are even slower than PS-d<sub>3</sub> in a given solvent, the viscosity exponent  $\alpha$  equals 1; i.e., Kramers' theory seems to be applicable for solutions of PNMA.

The above argument is further justified by work on small-molecule isomerization reactions. A functional form similar to eq 5 has been obtained theoretically for such reactions if the solvent is treated as viscoelastic. Grote and Hynes<sup>25</sup> generalized Kramers' theory by including the frequency dependence of the friction. Physically this means that the part of the viscosity

which arises from low-frequency motions does not impede motion across the barrier; thus the effective solvent friction in the barrier region is much smaller. Bagchi and Oxtoby<sup>26</sup> applied Grote and Hynes' theory to the rate of photochemical isomerization in solution. A power law dependence on solvent viscosity was found, with the solvent exponent ranging from 0.1 to 1. Recent work has extended this approach.<sup>27</sup>

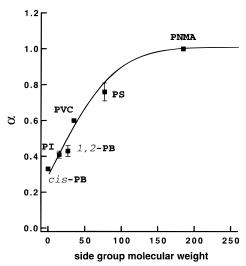
Another possible reason for the failure of eq 4 may lie in the traditional assumption that the rate of conformational transitions is inversely proportional to the characteristic time  $\langle \sigma \rangle$ . Recent computer simulations by Moe and Ediger<sup>28</sup> have raised doubts about this assumption. Although further investigation is required, our current speculation is that the changes in the relationship between transition rates and  $\langle \sigma \rangle$  do not account for the nonlinear viscosity dependence.

In the analysis above, we have only used data from the extreme narrowing regime and have not assumed any model for C-D vector reorientation. It is possible to check our conclusions by fitting all the NMR data (both in and out of the extreme narrowing regime) with a specific model. For this purpose we used the modified  $\log \chi^2$  model and calculated  $\langle \sigma \rangle$  by integrating the C–D vector correlation function extracted from the fitting. Details may be found elsewhere.<sup>7</sup> Using  $\langle \sigma \rangle$  values extracted from these fits, plots of log  $\langle \sigma \rangle$  vs log  $\eta$  give  $\alpha$ values of 0.78 at 420 K and 0.86 at 385 K. The activation energy  $E_{\rm a}$  obtained from the fitting is  $16\pm4$ kJ/mol, with 12 kJ/mol in toluene, 18 kJ/mol in cisdecalin, and 20 kJ/mol in DBP.

The model-dependent approach agrees with the modelindependent approach in a broad sense; i.e., eq 4 is not applicable to PS. In the model-independent approach, the extreme narrowing region can only be defined approximately. In the model-dependent approach, a particular model has to be assumed. This model is not necessarily correct and the fitting is not perfect. For the present, we have more confidence in the modelindependent approach.  $T_1$  measurements at a lower Larmor frequency should better define the extreme narrowing region and allow the discrepancy between the activation energies obtained from these two different approaches to be resolved.

Comparison of  $\alpha$  for Different Polymers. Although the theoretical prediction of  $\alpha$  is not possible at this time, it has been argued<sup>4</sup> previously that  $\alpha$  should depend upon three factors: the moment of inertia, the size of the isomerizing unit, and the curvature of the potential energy surface on the top of barrier. Bigger size, a bigger moment of inertia, and a smaller curvature all lead to a bigger  $\alpha$  (up to a limit of 1). While the curvature of the potential is difficult to determine from experimental measurements, the size and the moment of inertia of the isomerizing group correlate roughly with the molecular weight of the polymer side group. Thus we expect that  $\alpha$  should increase as the side group molecular weight increases. Figure 6 shows that this is the case. Eventually when the polymer has a very large side group such as poly(1-naphthylmethyl acrylate),  $\alpha = 1$  and Kramers' theory is applicable. In the absence of detailed experiments on a given polymer, we suggest that Figure 6 might provide a rough estimate of  $\alpha$ . The relationship between  $\alpha$  and side group mass might be different for quite flexible side groups.

Comparison to Other Work on PS Solutions. Two groups have previously investigated backbone segmental motions of PS in solution using NMR. Gron-



**Figure 6.** Viscosity exponent  $\alpha$  of various polymers vs side group molecular weight. As the molecular weight increases,  $\alpha$ increases until it reaches 1. The error bar for cis-PB is smaller than the symbol. The  $\alpha$  values for PVC and PNMA are model dependent and have undetermined error bars.  $\alpha$  is obtained from the following references: cis-PB, ref 3; PI, ref 4; 1,2-PB, ref 5; PVC(poly(vinyl chloride)), ref 6; PS, this work; PNMA (poly(1-naphthylmethyl acrylate)), ref 24. The line is drawn to guide the eye.

ski et al.  $^{21}$  used  $^{13}$ C NMR  $T_1$  measurements to study 1% PS in toluene and cyclohexane. Such low-concentration solutions could be studied because the PS was 50% <sup>13</sup>C enriched at backbone methine carbons. Assuming Kramers' theory, they obtained activation energies of 10.5 kJ/mol in toluene and 15 kJ/mol in cyclohexane. A reanalysis of their data using eq 5 with  $\alpha = 0.76$  gives an activation energy of 13 kJ/mol in toluene and 18 kJ/ mol in cyclohexane. Grandjean et al.29 performed 2H  $T_1$  experiments on 16% and 18% PS- $d_3$  in benzene and in diethyl malonate, respectively. They used Kramers' theory to obtain activation energies of 14 kJ/mol in benzene and 12 kJ/mol in diethyl malonate. Their data cover a limited temperature range and thus the activation energies have reasonably large errors. Reanalysis of these data using the nonlinear viscosity dependence yields an activation energy of 16 kJ/mol in both solvents. All these results are in reasonably agreement with those reported here. In the work reported in refs 21 and 29, specific models were employed to fit the data. It is not known whether other models would give the same results.

The use of Kramers' theory to describe the viscosity dependence of polymer local dynamics can lead to incorrect activation energies. For PS, the viscosity exponent is close to 1; therefore the errors in activation energy generated by assuming Kramers' theory are not large. For polymers with smaller viscosity exponents, <sup>3–5</sup> Kramers' theory can lead to substantial errors. For PS the dependence of  $E_a$  on solvent complicates any attempt to equate this quantity with a barrier in the bulk. For other polymers,  $E_a$  is often observed to be solvent independent.

Optical measurements have been performed by Waldow et al. on anthracene labeled PS in six solvents.<sup>30</sup> These PS molecules each contained one chromophore covalently bonded into the center of the chain backbone. Time-correlated single-photon counting was employed to monitor the chromophore (anthracene) reorientation in labeled chains. A viscosity exponent  $\alpha$  of 0.90  $\pm$  0.05 was found in these experiments. The different  $\alpha$  values

found in the optical and the NMR experiments are due to the presence of the chromophore in the optical experiments. Because of this, the length scale of the segmental motions detected in the optical experiments is somewhat larger than that in the NMR experiments (perhaps 5-10 repeat units in the optical experiments and 1-2 repeat units in the NMR experiments). Motion of larger portions of the chain leads to an  $\alpha$  closer to unity in the optical experiments. Qualitatively, this is similar to the trend shown in Figure 6. For polyisoprene, the viscosity exponent  $\alpha$  was determined to be 0.41 from the NMR measurements<sup>4</sup> and 0.76 from the optical measurements.31

## **IV. Summary**

Deuterium  $T_1$  measurements have been performed on backbone-deuterated PS- $d_3$  in four solvents. The time integral of the C-D vector orientation correlation function  $\langle \sigma \rangle$  has been extracted from  $T_1$  measurements model independently. In contrast to the prediction of Kramers' theory in the high-friction limit,  $\langle \sigma \rangle$  is found to be proportional to solvent viscosity  $\eta$  raised to the 0.76  $\pm$ 0.05 power, whether the viscosity is varied by changing the temperature or solvent. A very similar result is obtained if the  $T_1$  measurements are analyzed using a model for the description of C–D vector reorientation. These results fit in well with results from the literature and indicate that the viscosity exponent increases with the mass of the polymer side group.

The internal energy barrier  $E_a$  associated with C-D vector orientation was found to be  $14 \pm 3$  kJ/mol. The systematic dependence of  $E_a$  upon the solvent identity was not expected and is in contrast to the behavior observed for polyisoprene, cis-1,4-polybutadiene, and 1,2-polybutadiene.

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**Supporting Information Available:**  $T_1$  data for PS- $d_3$ in toluene, cis-decalin, dibutyl phthalate, and dioctyl phthalate at 15.37 and 76.86 MHz (5 pages). Ordering information is given on any current masthead page.

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